FOR EDEXCEL

## GCE Examinations Advanced Subsidiary

## **Core Mathematics C3**

Paper C

Time: 1 hour 30 minutes

## Instructions and Information

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration.

Full marks may be obtained for answers to ALL questions.

Mathematical formulae and statistical tables are available.

This paper has eight questions.

## Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working may gain no credit.



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1	(a)	Evnrace
ı.	(a)	Express

$$\frac{x+4}{2x^2+3x+1} - \frac{2}{2x+1}$$

as a single fraction in its simplest form.

**(3)** 

Hence, find the values of *x* such that (b)

$$\frac{x+4}{2x^2+3x+1} - \frac{2}{2x+1} = \frac{1}{2}.$$
 (3)

2. Prove, by counter-example, that the statement (a)

"cosec  $\theta - \sin \theta > 0$  for all values of  $\theta$  in the interval  $0 < \theta < \pi$ "

is false. **(2)** 

Find the values of  $\theta$  in the interval  $0 < \theta < \pi$  such that

$$\csc \theta - \sin \theta = 2$$
,

giving your answers to 2 decimal places.

**(5)** 

**(3)** 

**(5)** 

**3.** Solve each equation, giving your answers in exact form.

(a) 
$$\ln(2x-3) = 1$$

(b) 
$$3e^y + 5e^{-y} = 16$$
 (5)

4. Differentiate each of the following with respect to *x* and simplify your answers.

(a) 
$$\ln(3x-2)$$

(b) 
$$\frac{2x+1}{1-x}$$

(c) 
$$x^{\frac{3}{2}}e^{2x}$$

5.

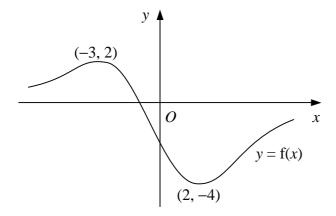


Figure 1

Figure 1 shows the curve y = f(x) which has a maximum point at (-3, 2) and a minimum point at (2, -4).

- (a) Showing the coordinates of any stationary points, sketch on separate diagrams the graphs of
  - (*i*) y = f(|x|),

$$(ii) \quad y = 3f(2x). \tag{7}$$

- (b) Write down the values of the constants a and b such that the curve with equation y = a + f(x + b) has a minimum point at the origin O. (2)
- **6.** The function f is defined by

$$f(x) \equiv 4 - \ln 3x, \quad x \in \mathbb{R}, \quad x > 0.$$

(a) Solve the equation 
$$f(x) = 0$$
. (2)

(b) Sketch the curve 
$$y = f(x)$$
. (2)

(c) Find an expression for the inverse function, 
$$f^{-1}(x)$$
. (3)

The function g is defined by

$$g(x) \equiv e^{2-x}, \quad x \in \mathbb{R}.$$

(d) Show that

$$fg(x) = x + a - \ln b,$$

where a and b are integers to be found.

Turn over

**(3)** 

- 7. (a) Express  $4 \sin x + 3 \cos x$  in the form  $R \sin (x + \alpha)$  where R > 0 and  $0 < \alpha < \frac{\pi}{2}$ .
  - (b) State the minimum value of  $4 \sin x + 3 \cos x$  and the smallest positive value of x for which this minimum value occurs. (3)
  - (c) Solve the equation

$$4\sin 2\theta + 3\cos 2\theta = 2,$$

for  $\theta$  in the interval  $0 \le \theta \le \pi$ , giving your answers to 2 decimal places. (6)

- **8.** The curve C has the equation  $y = \sqrt{x} + e^{1-4x}$ ,  $x \ge 0$ .
  - (a) Find an equation for the normal to the curve at the point  $(\frac{1}{4}, \frac{3}{2})$ . (4)

The curve C has a stationary point with x-coordinate  $\alpha$  where  $0.5 < \alpha < 1$ .

(b) Show that  $\alpha$  is a solution of the equation

$$x = \frac{1}{4} [1 + \ln(8\sqrt{x})]. \tag{3}$$

**(2)** 

(c) Use the iteration formula

$$x_{n+1} = \frac{1}{4} [1 + \ln(8\sqrt{x_n})],$$

with  $x_0 = 1$  to find  $x_1, x_2, x_3$  and  $x_4$ , giving the value of  $x_4$  to 3 decimal places. (3)

- (d) Show that your value for  $x_4$  is the value of  $\alpha$  correct to 3 decimal places. (2)
- (e) Another attempt to find  $\alpha$  is made using the iteration formula

$$x_{n+1} = \frac{1}{64} e^{8x_n-2}$$
,

with  $x_0 = 1$ . Describe the outcome of this attempt.

**END**